

# Fuzzy Logic and Fuzzy Algorithms

CISC871/491

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## Presentation Outline

- Fuzzy control system
- Fuzzy Traffic controller
- Modeling and Simulation
- Hardware Design
- Conclusion

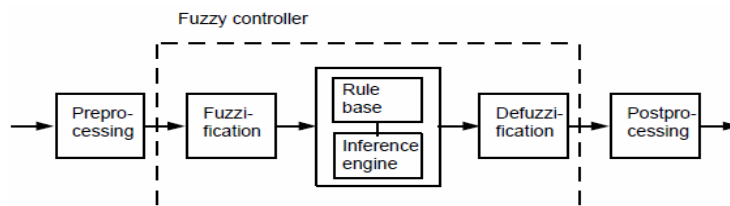
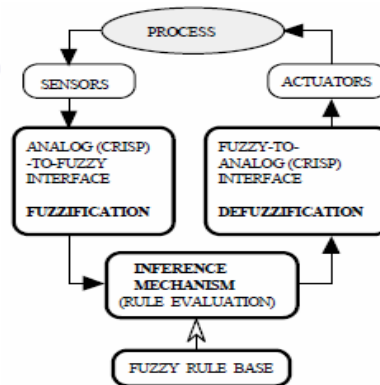


# Fuzzy Control System

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## Fuzzy Control

Fuzzy control provides a formal methodology for representing, manipulating, and implementing a human's heuristic knowledge about how to control a system.



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Figure from Prof. Emil M. Petriu, University of Ottawa

# Advantage

## Useful cases:

- The control processes are **too complex to analyze** by conventional quantitative techniques.
- The available **sources of information are interpreted qualitatively, inexactly, or uncertainly.**
- **Embedded design & control, Industrial control, Robot control etc**

## Advantages of FLC:

- **Parallel or distributed control multiple fuzzy rules** – complex nonlinear system
- Linguistic control. Linguistic terms - human knowledge
- Robust control. More than 1 control rules – a error of a rule is not fatal.

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# Basic Structure of Controller

## FUZZIFIER

Fuzzifier takes the crisp inputs to a fuzzy controller and converts them into fuzzy inputs.

## FUZZY RULE BASE (Knowledge base)

It consists of fuzzy **IF-THEN rules** that form the heart of a fuzzy inference system. A fuzzy rule base is comprised of canonical fuzzy IF-THEN rules of the form IF  $x_1$  is  $A_1(l)$  and ... and  $x_n$  is  $A_n(l)$  THEN  $y$  is  $B(l)$ , where  $l = 1, 2, \dots, M$ . Should have Completeness, Consistency, Continuity..

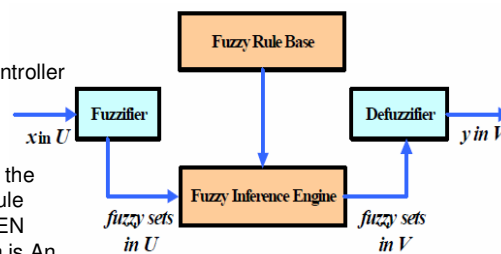
## FUZZY INFERENCE ENGINE

Fuzzy Inference Engine makes use of fuzzy logic principles to combine the fuzzy IF-THEN rules. Composition based inference (**Max/Min, Max/Product**) and individual-rule based inference (**Mamdani**). Other methods like **Tsukamoto, Takagi Sugeno Kang (TSK)**

## DEFUZZIFIER

– It extracts a crisp value from a fuzzy set.

- Smallest of Maximum.
- Largest of Maximum.
- **Centroid of area.**
- Bisector of Area
- Mean of maximum.

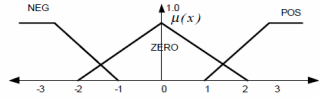


General model of a Fuzzy system.

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# Example

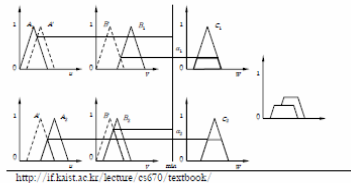
$$\mu_{pos}(x) = \begin{cases} 1 & \text{if } x \geq 3 \\ \frac{x-1}{2} & \text{if } 1 \leq x < 3 \\ 0 & \text{otherwise} \end{cases}$$



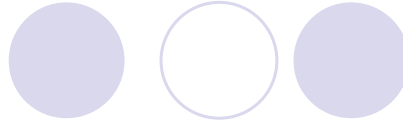
Membership functions of positive, zero and negative numbers.

Inference method: Mamdani

- minimum operator for a fuzzy implication
- max-min operator for the composition



<http://if.kaist.ac.kr/lecture/cs670/textbook/>



Rule base design. Types of fuzzy control rules.

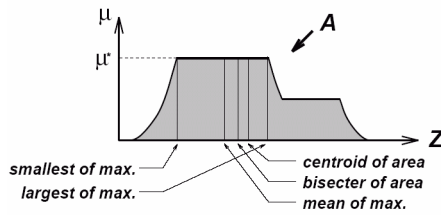
A set of fuzzy rules

$R_i$ : if  $x$  is  $A_i$ , and  $y$  is  $B_i$ , then  $z$  is  $C_i$ ,  $i = 1, 2, \dots, n$

Can be represented as a rule table

$B_0$				$C_0$
$\dots$		$C_5$	$C_6$	$C_6$
$B_2$		$C_3$	$C_4$	$C_4$
$B_1$	$C_1$	$C_2$	$\dots$	$C_7$
	$A_1$	$A_2$	$\dots$	$A_n$

<http://if.kaist.ac.kr/lecture/cs670/textbook/>



"Fuzzy Control" Kevin M. Passino and Stephen Yurkovich  
<http://if.kaist.ac.kr/lecture/cs670/textbook/>

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# Fuzzy Traffic controller

## A Design Methodology for the Implementation of a Fuzzy Logic Traffic Controller Using FPGA Technology

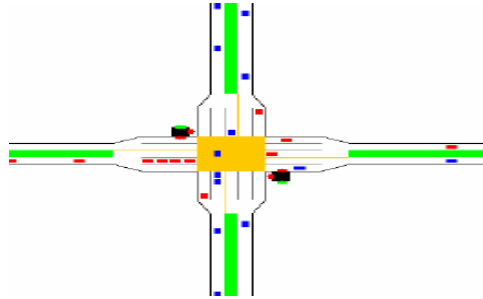
Mandar Ambre, Bing W.Kwan and Leonard J.Tung  
Department of Electrical & Computer Engineering  
FAMU-FSU College of Engineering, Florida State University  
THE HUNTSVILLE SIMULATION CONFERENCE HSC 2003

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# Overview

## Goal

- Improving Safety
- Balanced traffic flow
- Minimizing travel time
- Increasing the capacity

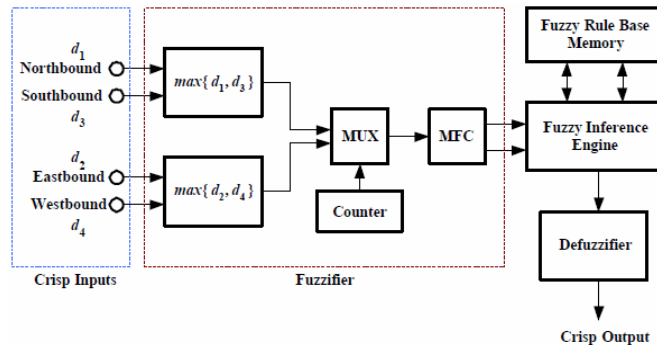
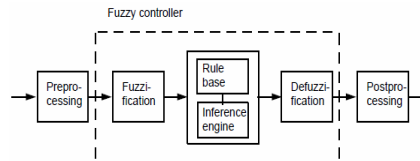


## Why Fuzzy traffic controller

- No obvious optimal solution
- Most traffic has fixed cycle controllers that need manual changes to adapt specific situation
- One of the desirable features of traffic controllers is to dynamically effect the change of signal phase durations
- This problem can be solved by use of fuzzy traffic controllers which are capable of signaling adaptively at an intersection.

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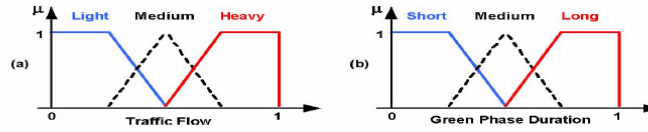
# Traffic Controller Case example



Basic configuration of the fuzzy logic traffic controller

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# Membership functions and Fuzzy Rule Base



(a) Membership functions for the fuzzy sets, Light, Medium, and Heavy, which are induced by the traffic-queue deviations. (b) Membership functions for fuzzy sets, Short, Medium, and Long, which label the green phase duration.

Fuzzy IF-THEN rules for traffic control

	Traffic Flow Condition								
NS-bound traffic	Light	Light	Light	Med	Med	Med	Heavy	Heavy	Heavy
EW-bound traffic	Light	Med	Heavy	Light	Med	Heavy	Light	Med	Heavy
NS green phase	Short	Short	Short	Med	Med	Med	Long	Long	Long
EW green phase	Short	Med	Long	Short	Med	Long	Short	Med	Long
	Duration								

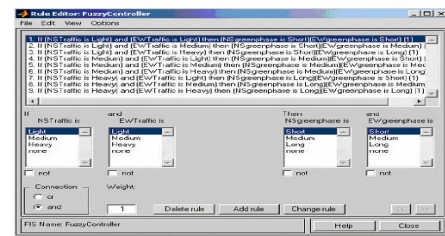
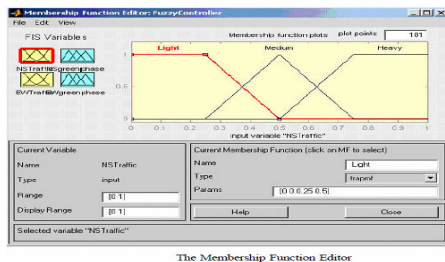
IF (NS-bound traffic is Medium) THEN (NS green phase duration is Medium)

IF (EW-bound traffic is Light) THEN (EW green phase duration is Short)

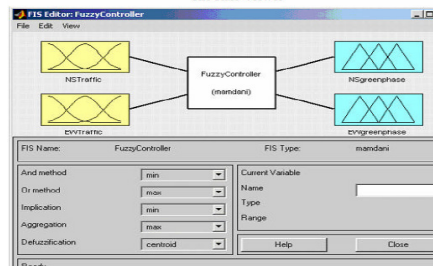
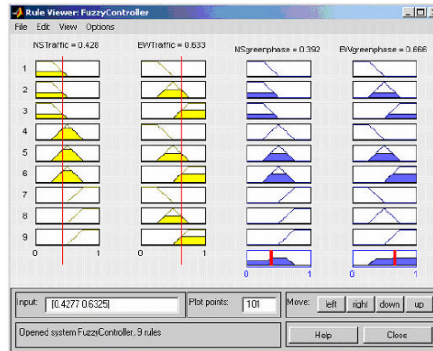
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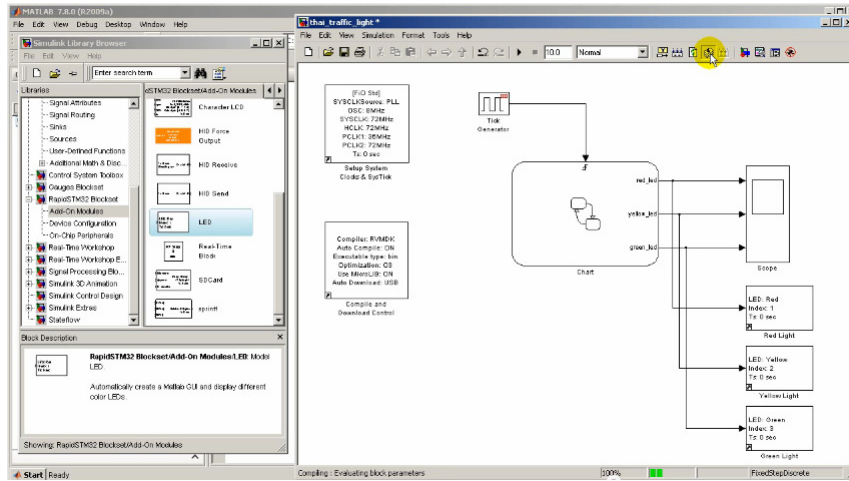
# MATLAB



<http://www.mathworks.com/help/toolbox/fuzzy/fp243d.ip9.html>



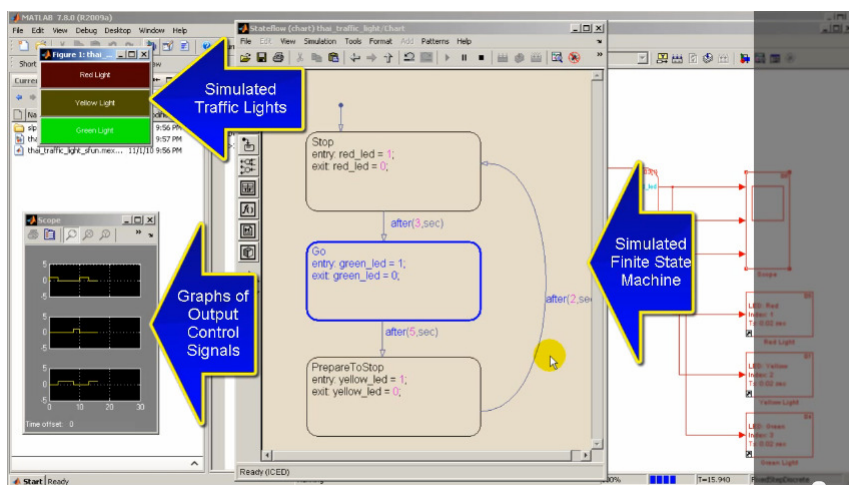
# Modeling example (Simulink)



<http://www.youtube.com/watch?v=hFWGTol-Nhw>  
<http://www.mathworks.com/products/simulink/demos.html>

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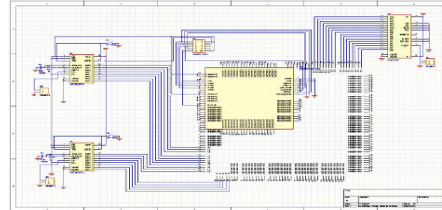
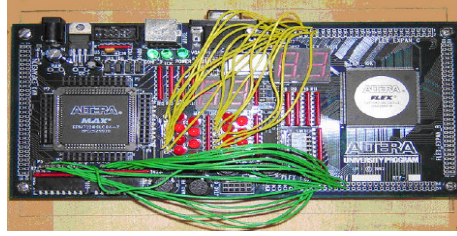
# Modeling using Simulink (Cont.)



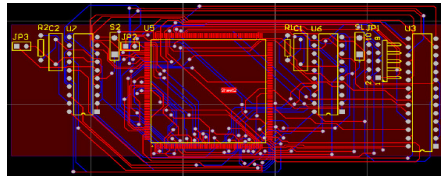
<http://www.youtube.com/watch?v=hFWGTol-Nhw>  
<http://www.mathworks.com/products/simulink/demos.html>

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## Hardware Design



Schematic Document for the circuit



## Conclusion

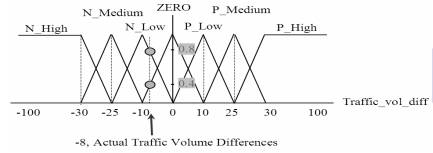
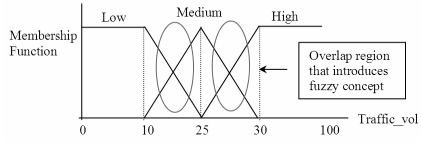
- ✓ Overview of Fuzzy Controller basic theory
- ✓ Case Study of Fuzzy Traffic Controller Design
- ✓ Discuss about Simulation Environment
- ✓ Hardware Implementation Issue

### Further Improvement

- Evolving Fuzzy system
- Utilize genetic algorithm
- Use Dynamic inputs
- Advanced EDE tools (H/W)

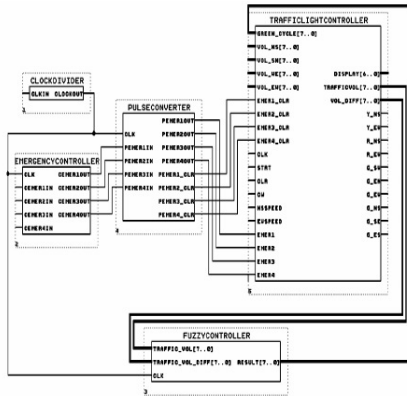
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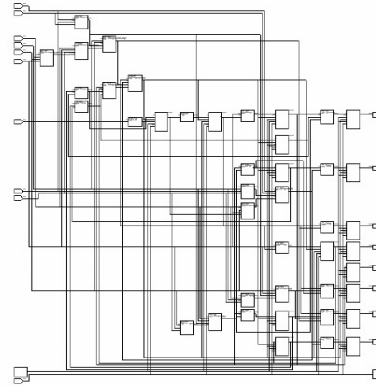


## Case Study 2 (Extra)

TRAFFIC VOLUME	TRAFFI_VOL_DIFF = ACTIVE LANE TRAFFIC - AVERAGE WAITING TRAFFIC						
	F_HIGH	F_MEDIUM	F_LOW	ZERO	N_LOW	N_MEDIUM	N_HIGH
HIGH	F_HIGH	F_MEDIUM	HIGH	HIGH	HIGH	N_MEDIUM	N_HIGH
MEDIUM	F_HIGH	MEDIUM	MEDIUM	MEDIUM	MEDIUM	MEDIUM	N_HIGH
LOW	F_HIGH	LOW	LOW	LOW	LOW	LOW	N_HIGH



Fuzzy traffic controller-interconnection of the entire modules



Fuzzy traffic controller gate level